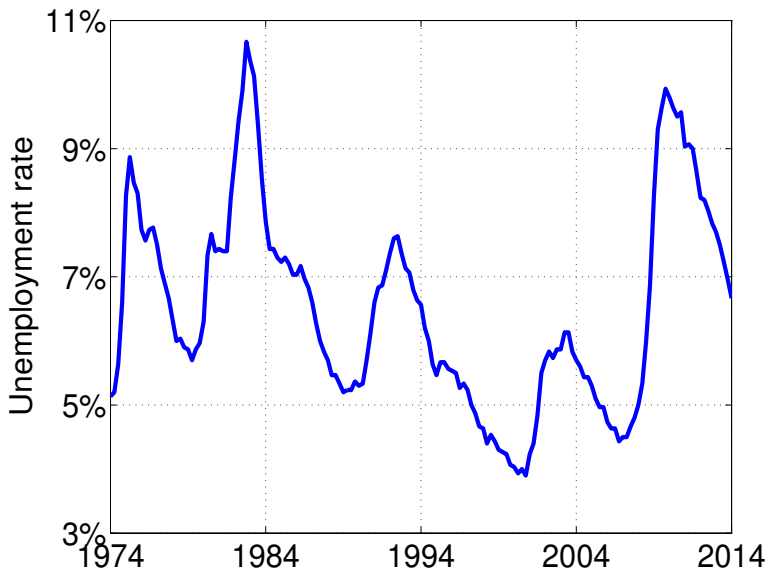


# Aggregate Demand, Idle Time, and Unemployment

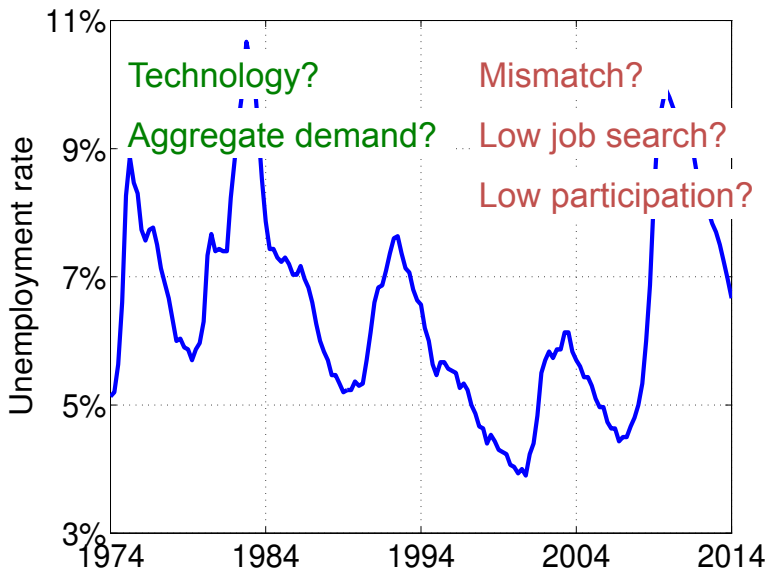
Pascal Michaillat (LSE) & Emmanuel Saez (Berkeley)

September 2014

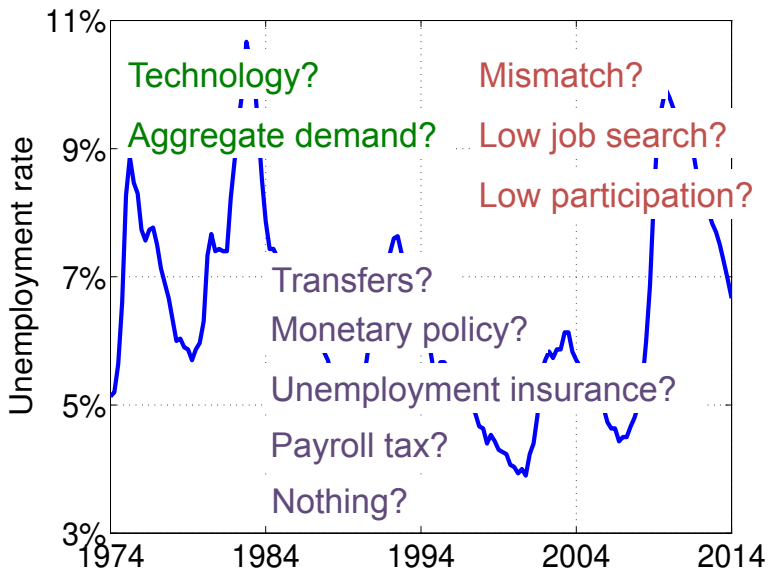
# Motivation



# Motivation



# Motivation



# The available models

## 1. matching model of the labor market

- ▶ tractable
- ▶ but no aggregate demand

## 2. ?

## 3. New Keynesian DSGE model

- ▶ many shocks
- ▶ but greater complexity

# The general disequilibrium model?

- vast literature after Barro & Grossman [1971]
- recent revival after Great Recession
  - Mankiw & Weinzierl [2011]
  - Caballero & Farhi [2014]
- captures important intuitions
- but difficult to analyze

# This model

equilibrium version of the Barro-Grossman model, with **matching frictions** on product + labor markets:

- graphical representation of GE and welfare
- frictional + classical + Keynesian unemployment

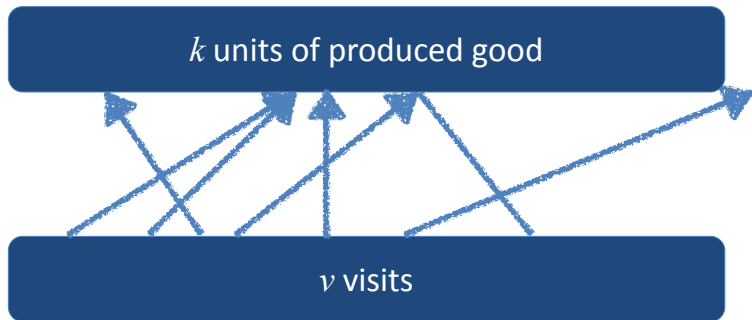
# Basic model (no labor market)



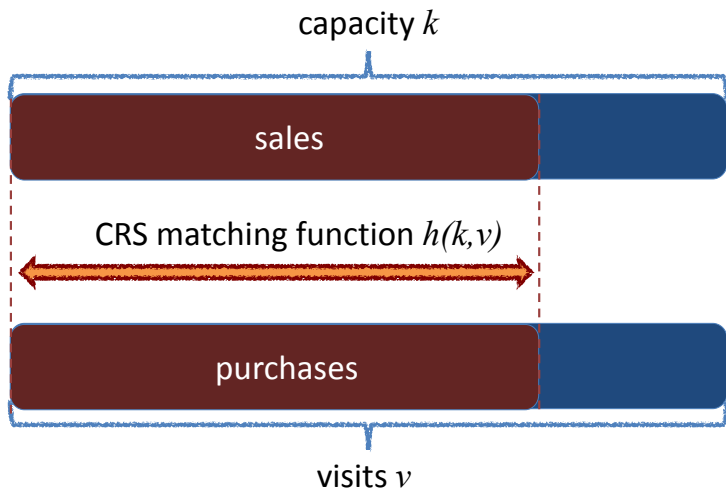
# Setup

- static model
- measure 1 of identical households
- production takes place within households
- households cannot consume own production
- households trade production on frictional market

# Matching function and tightness



# Matching function and tightness



# Matching function and tightness

$$\text{tightness: } x = v / k$$

capacity  $k$

$$\text{sales} = k \cdot h(1, x) = k \cdot f(x_+)$$

$$\text{output: } y = h(k, v)$$

$$\text{purchases} = v \cdot h\left(\frac{1}{x}, 1\right) = v \cdot q(x_-)$$

visits  $v$

# Low product market tightness



# High product market tightness



# Matching cost: $\rho$ goods per visit

- output =  $\left[1 + \tau(x)_+\right] \cdot \text{consumption}$

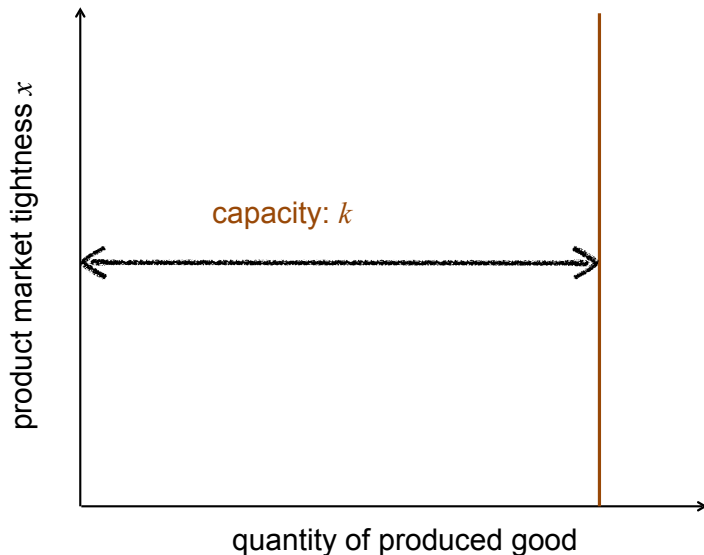
- proof:

$$\underbrace{y}_{\text{output}} = \underbrace{c}_{\text{consumption}} + \underbrace{\rho \cdot v}_{\text{trading}} = c + \rho \cdot \frac{y}{q(x)}$$

$$\Rightarrow y \cdot \left[1 - \frac{\rho}{q(x)}\right] = c$$

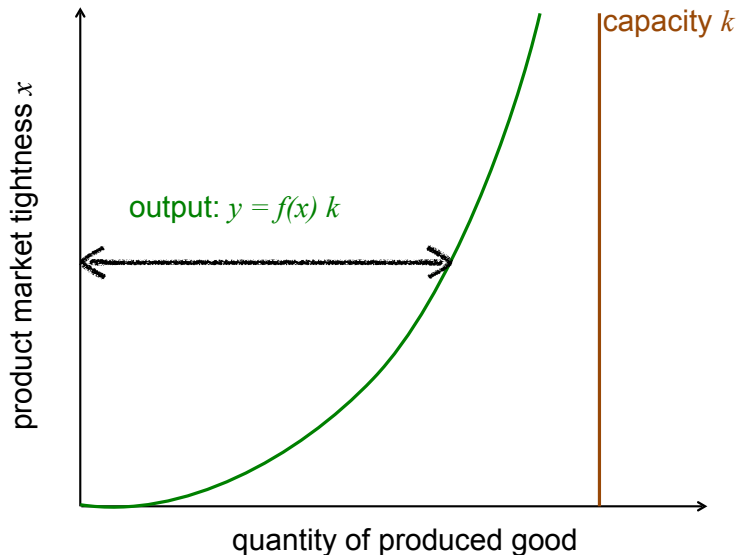
$$\Rightarrow y = \left[1 + \frac{\rho}{q(x)_- - \rho}\right] \cdot c \equiv \left[1 + \tau(x)_+\right] \cdot c$$

# Tightness and aggregate supply

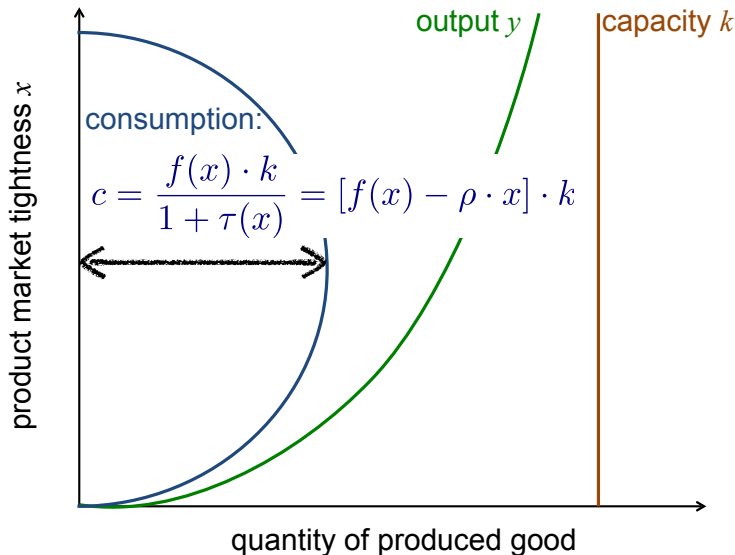




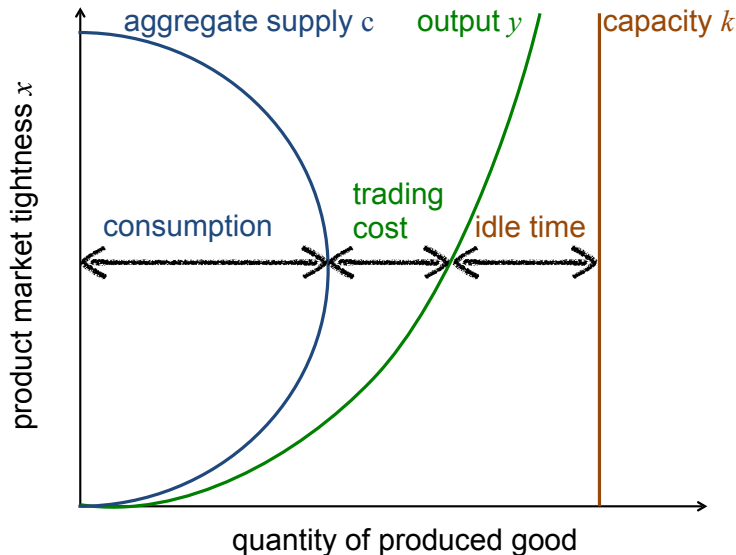
# Tightness and aggregate supply



# Tightness and aggregate supply



# Tightness and aggregate supply



# Nonproduced good

- valued by consumers
- in fixed supply
- traded on a perfectly competitive market
- examples: real money, land, gold, fixed capital
- as in Barro & Grossman [1971], Hart [1982], and Blanchard & Kiyotaki [1987]

# Households

- take price  $p$  and tightness  $x$  as given
- choose  $c$ ,  $m$  to maximize utility

$$\left( \underbrace{\frac{\chi}{1+\chi} \cdot c^{\frac{\varepsilon-1}{\varepsilon}}}_{\text{produced good}} + \underbrace{\frac{1}{1+\chi} \cdot m^{\frac{\varepsilon-1}{\varepsilon}}}_{\text{nonproduced good}} \right)^{\frac{\varepsilon}{\varepsilon-1}}$$

- subject to budget constraint

$$\underbrace{m}_{\text{numeraire}} + p \cdot \underbrace{(1 + \tau(x)) \cdot c}_{\text{produced good}} = \underbrace{\mu}_{\text{endowment}} + \underbrace{f(x) \cdot p \cdot k}_{\text{labor income}}$$

# Optimal consumption decision

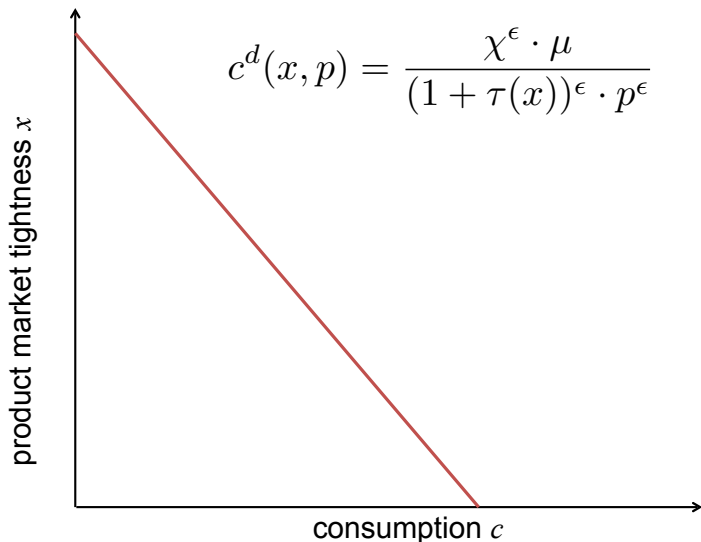
- first-order condition

$$\underbrace{(1 + \tau(x)) \cdot p}_{\text{product price}} \cdot \underbrace{\frac{1}{1 + \chi} \cdot m^{-\frac{1}{\varepsilon}}}_{\text{MU of nonproduced good}} = \underbrace{\frac{\chi}{1 + \chi} \cdot c^{-\frac{1}{\varepsilon}}}_{\text{MU of produced good}}$$

- aggregate demand (as  $m = \mu$ ):

$$c^d(x, p) = \frac{\chi^\varepsilon \cdot \mu}{(1 + \tau(x))^\varepsilon \cdot p^\varepsilon}$$

# Tightness and aggregate demand



# Definition of equilibrium

- equilibrium is  $(x, p)$  such that supply = demand:

$$c^s(x) = c^d(x, p)$$

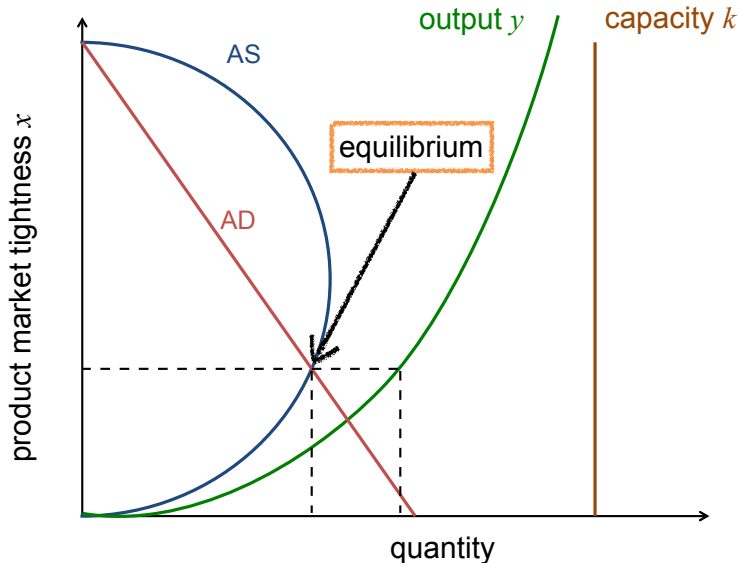
- 1 equation, 2 variables: indeterminacy
- need a price mechanism to select equilibrium
  - ▶ fixed price
  - ▶ efficient price



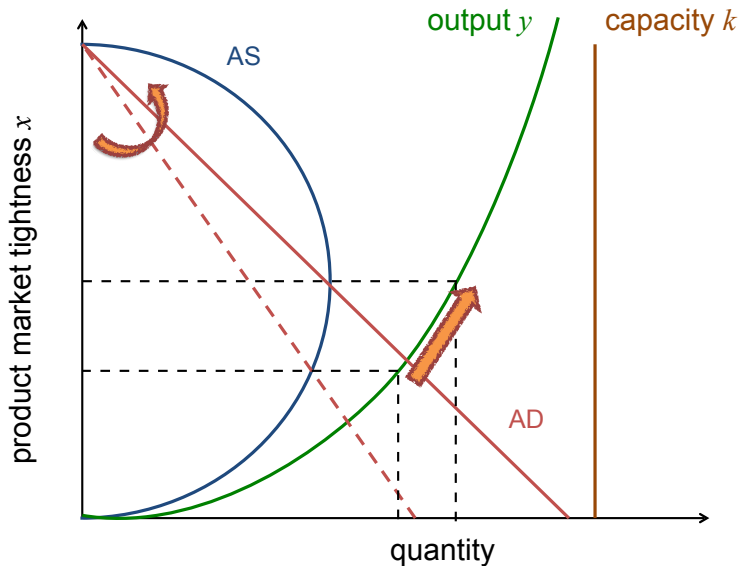
# Comparative statics

## with fixed price and efficient price

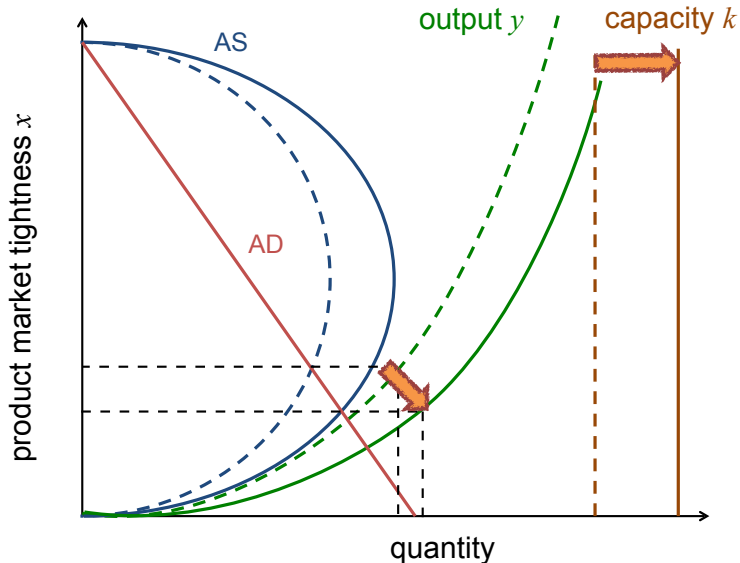
# Increase in AD with fixed price



# Increase in AD with fixed price



# Increase in AS with fixed price



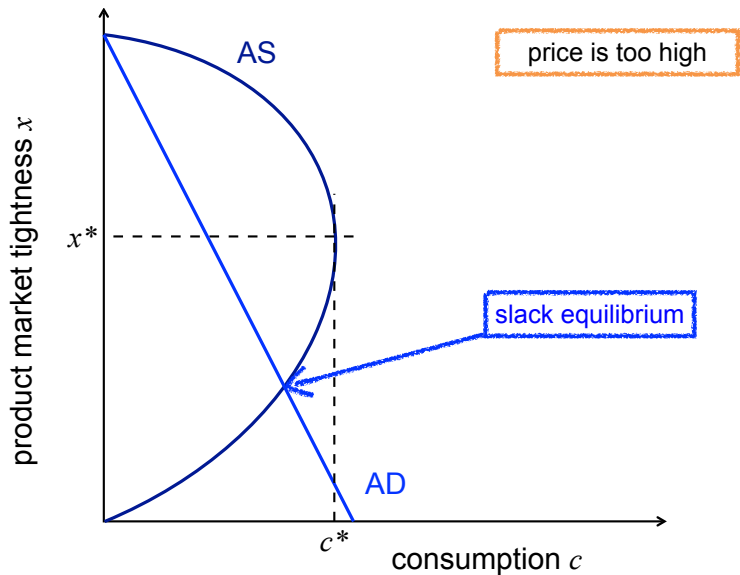
# Comparative statics with fixed price

---

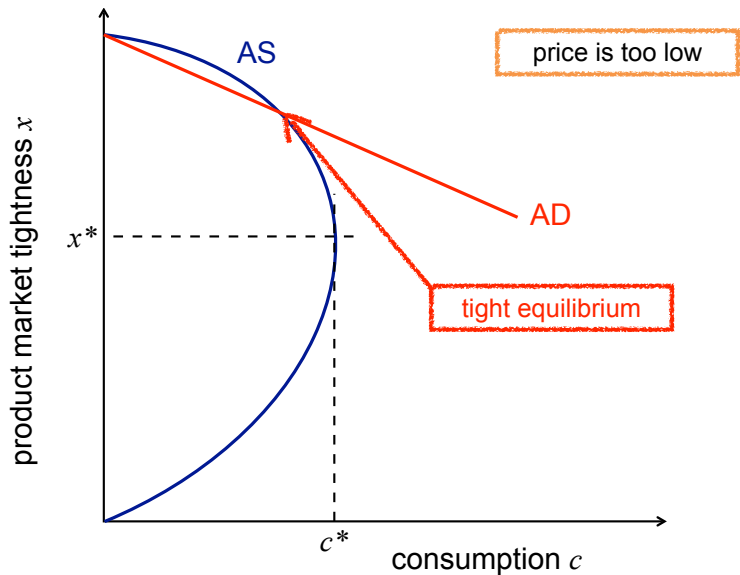
	effect on:	
	output	tightness
increase in:	$y$	$x$
aggregate demand	+	+
aggregate supply	+	—

---

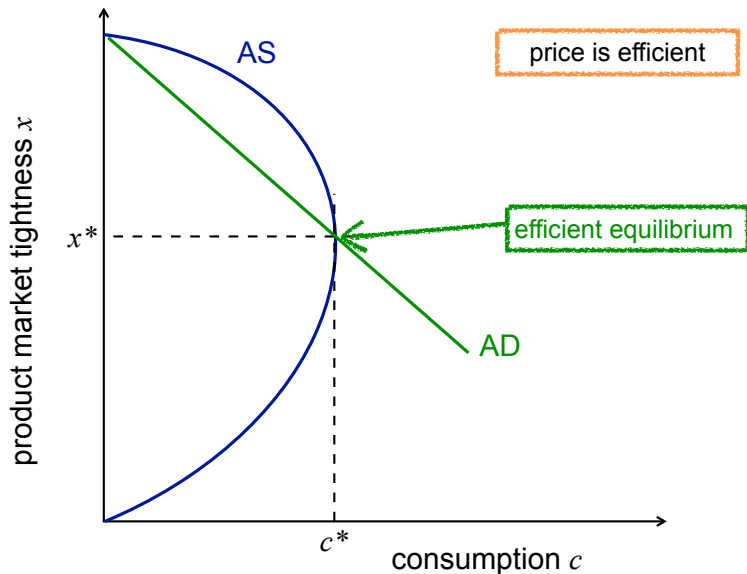
# Definition of efficient price



# Definition of efficient price



# Definition of efficient price





# Comparative statics with efficient price

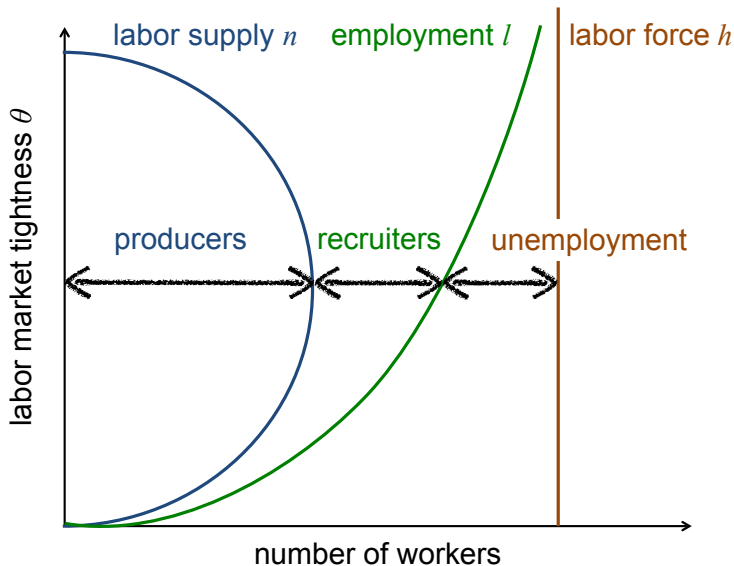
---

	effect on:	
	output	tightness
increase in:	$y$	$x$
aggregate demand	0	0
aggregate supply	+	0

---

# Complete model

# Labor market and unemployment



# Firms

- employ producers and recruiters and sell production
- take real wage  $w$  and tightnesses  $x$  and  $\theta$  as given
- choose number of producers  $n$  to maximize profits

$$\underbrace{f(x)}_{\text{selling probability}} \cdot \underbrace{a \cdot n^{\alpha}}_{\text{production}} - \underbrace{[1 + \hat{\tau}(\theta)] \cdot w \cdot n}_{\text{wage of producers + recruiters}}$$

# Optimal employment decision

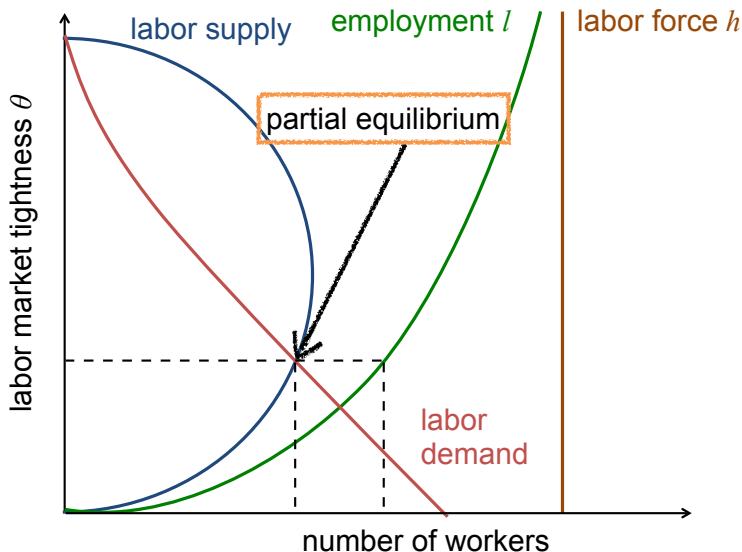
- first-order condition:

$$\underbrace{f(x)}_{\text{selling probability}} \cdot \underbrace{\alpha \cdot a \cdot n^{\alpha-1}}_{\text{MPL}} = \underbrace{[1 + \hat{\tau}(\theta)]}_{\text{matching wedge}} \cdot \underbrace{w}_{\text{real wage}}$$

- labor demand: demand for producers

$$n^d(\theta, x, w) = \left[ \frac{f(x) \cdot a \cdot \alpha}{(1 + \hat{\tau}(\theta)) \cdot w} \right]^{\frac{1}{1-\alpha}}$$

# Partial equilibrium on labor market



# General equilibrium $(x, \theta, p, w)$

- supply = demand on product and labor markets

$$\begin{cases} c^s(x, \theta) &= c^d(x, p) \\ n^s(\theta) &= n^d(\theta, x, w) \end{cases}$$

- 2 equations, 4 variables: indeterminacy
- need price and wage mechanisms

# Keynesian, classical, and frictional unemployment

- equilibrium employment:

$$l = \left( \frac{f(x) \cdot a \cdot \alpha}{w} \right)^{\frac{1}{1-\alpha}} \cdot \left( \frac{1}{1 + \hat{\tau}(\theta)} \right)^{\frac{\alpha}{1-\alpha}}$$

- frictional unemployment from  $\hat{\tau}(\theta) > 0$
- classical unemployment from  $w > a \cdot \alpha$
- **Keynesian unemployment from  $f(x) < 1$**



# Comparative statics with fixed prices

increase in:	effect on:			
	product		labor	
	output	tightness	tightness	employment
	$y$	$x$	$\theta$	$l$
aggregate demand	+	+	+	+
technology	+	—	+	+
labor supply	+	—	—	+
mismatch	—	+	+	—

# Comparative statics with fixed prices

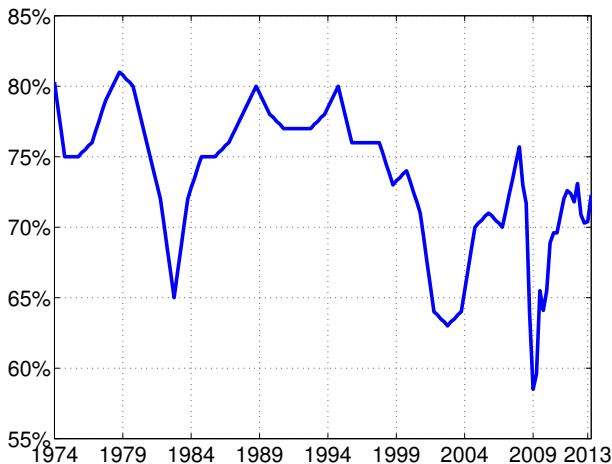
increase in:	effect on:			
	product		labor	
	output	tightness	tightness	employment
	$y$	$x$	$\theta$	$l$
aggregate demand	+	+	+	+
technology	+	-	+	+
labor supply	+	-	-	+
mismatch	-	+	+	-

# Comparative statics with efficient prices

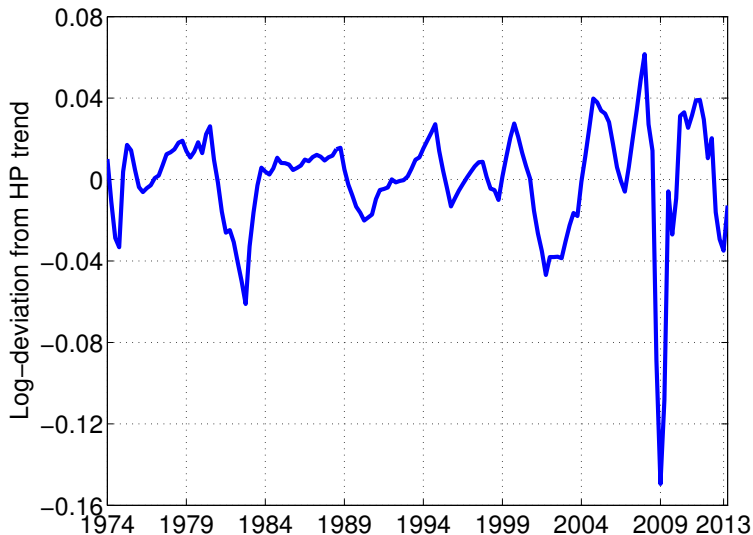
	effect on:			
	product		labor	
	output	tightness	tightness	employment
increase in:	$y$	$x$	$\theta$	$l$
aggregate demand	0	0	0	0
technology	+	0	0	0
labor supply	+	0	0	+
mismatch	—	0	0	—

Rigid or flexible prices?

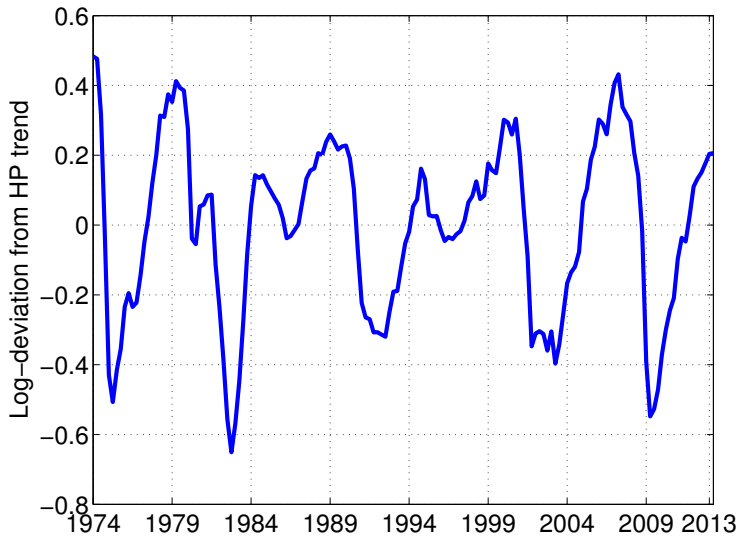
Construct proxy for product market tightness from  
capacity utilization measure in Survey of Plant Capacity:



## Fluctuations in product market tightness: rigid price



## Fluctuations in labor market tightness: rigid real wage

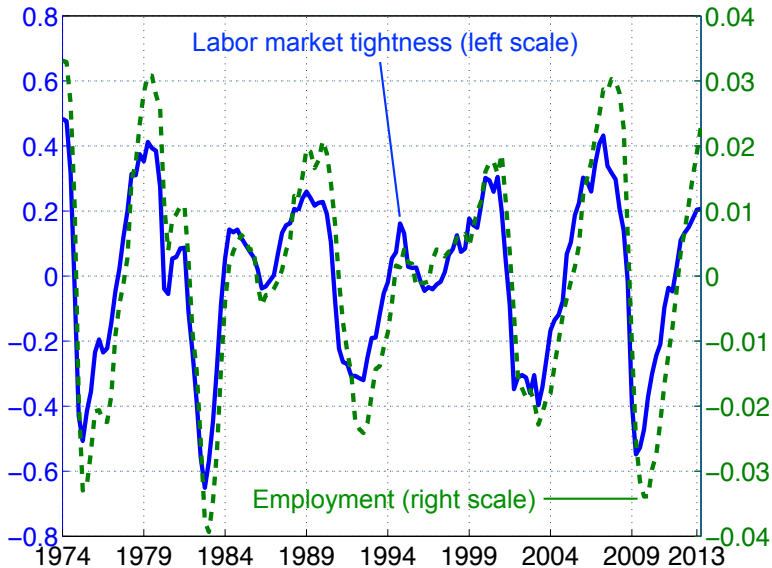


# Effect of labor supply and demand shocks

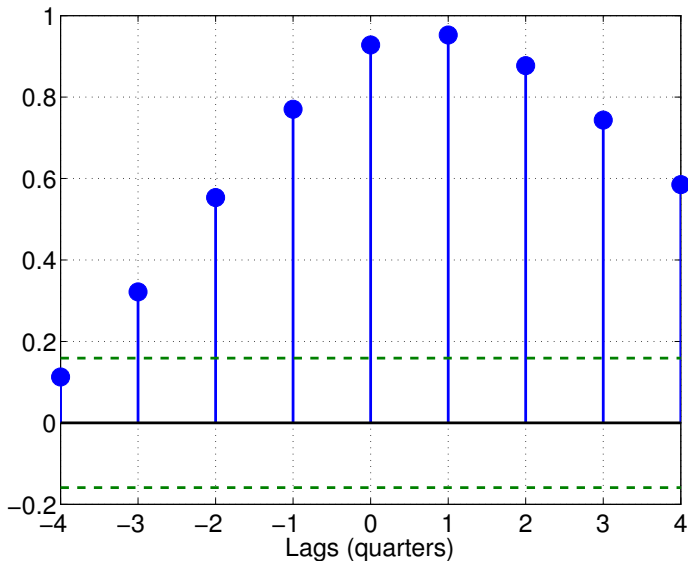
- labor **supply** shocks: **negative** correlation between employment and labor market tightness
- labor **demand** shocks: **positive** correlation between employment and labor market tightness



# Evidence of labor demand shocks



## Cross-correlogram: labor market tightness and employment

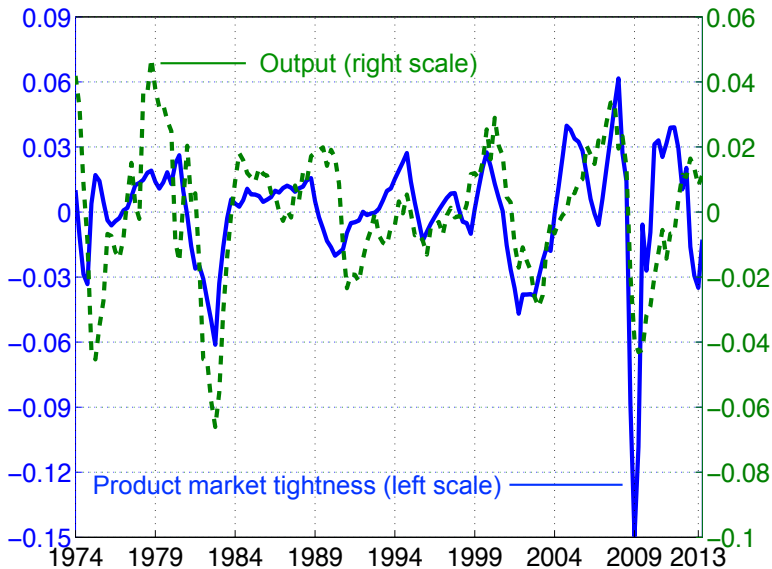


Labor demand shocks:  
AD or technology shocks?

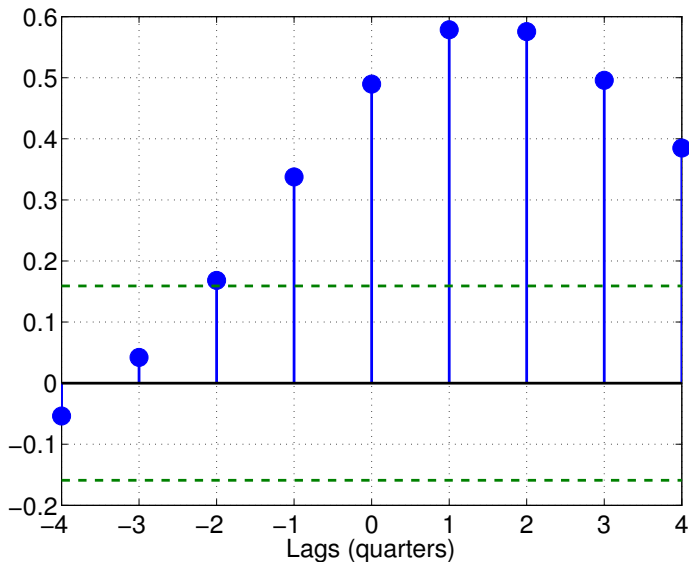
# Effect of AD and technology shocks

- **AD** shocks: **positive** correlation between output and product market tightness
- **technology** shocks: **negative** correlation between output and product market tightness

# Evidence of AD shocks



## Cross-correlogram: product market tightness and output



# Conclusion

- tractable model of unemployment fluctuations
- empirical series to measure tightness
  - ▶ product market tightness
  - ▶ labor market tightness
- origins of unemployment fluctuations
  1. importance of price and wage rigidity (not flexibility)
  2. importance of labor demand shocks (not labor supply)
  3. importance of AD shocks (not technology)